



APPLICATIONS WITH PARABOLIC FUNCTIONS (DAY 7)

EX. 1 Using the graph at the right, It shows the **height h** in feet of a small rocket **t seconds** after it is launched.

The path of the rocket is given by the equation:

$$h = -16t^2 + 128t.$$

1. How long is the rocket in the air? 8 seconds

2. What is the greatest height the rocket reaches? 256 ft

$$x = \frac{-b}{2a} \quad x = \frac{-128}{2(-16)} = 4 \quad -16(4)^2 + 128(4) = 256 \text{ ft}$$

3. About how high is the rocket after 1 second? 100 ft

4. After 2 seconds,
about how high is the rocket? 190 ft

is the rocket going up or going down? up

5. After 6 seconds,
about how high is the rocket? 190 ft

is the rocket going up or going down? down

6. Do you think the rocket is traveling faster from 0 to 1 second or from 3 to 4 seconds?
Explain your answer.

bc it grows by about 100 ft as opposed to about 20 ft from 3-4 sec

7. Using the equation, find the **exact** value of the height of the rocket at 2 seconds.

$$-16(2)^2 + 128(2) = \underline{192 \text{ ft}}$$

8. What is the domain of the graph?

$[0, 8]$ $0 \leq x \leq 8$ from 0 to 8

9. What is the range of the graph?

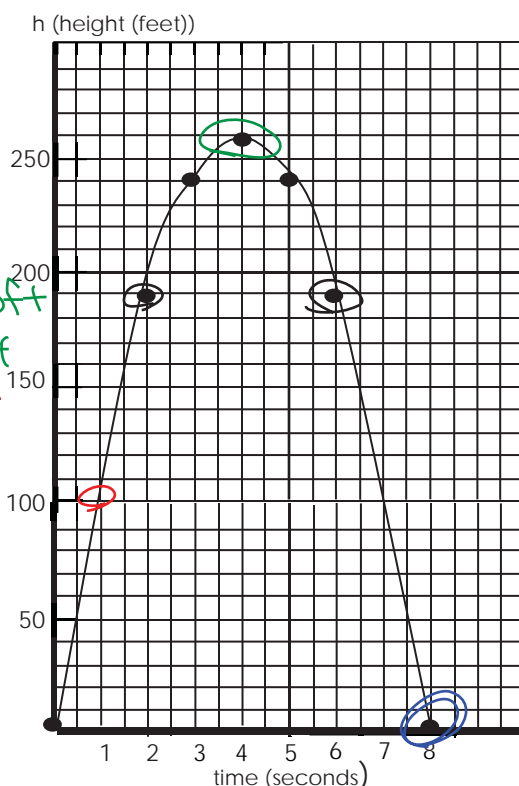
$[0, 256]$ $0 \leq y \leq 256$ from 0 to 256

10. Express the interval over which the graph is increasing.

$[0, 4)$

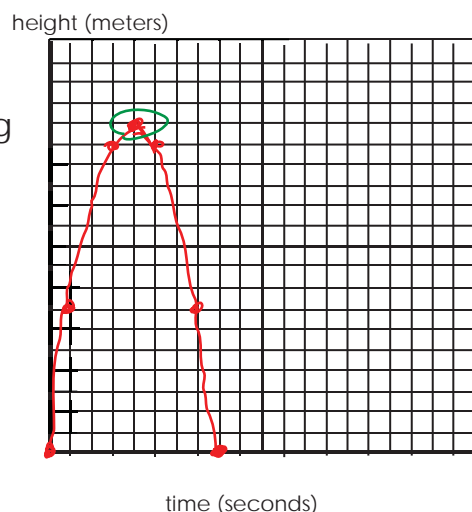
11. Express the interval over which the graph is decreasing.

$(4, 8]$





EX2: A ball is thrown in the air. The path of the ball is represented by the equation $h = -t^2 + 8t$. Graph the equation over the interval $0 \leq t \leq 8$ on the accompanying grid.

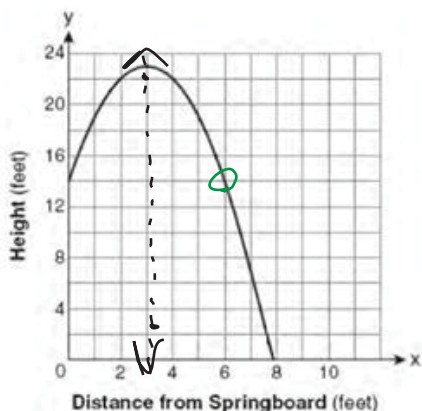


a) What is the maximum height of the ball? 16 meters

$$x = \frac{-8}{2(-1)} = 4 \quad - (4)^2 + 8(4) = 16$$

b) What is the amount of time that the ball is above 7 meters? 6 seconds

EX3: A swim team member performs a dive from a 14-foot high springboard. The parabola below shows the path of her dive.



a) What is the axis of symmetry? $x = 3$

b) Find $f(6)$ 14 ft

EX4: Consider the graph of the equation $y = ax^2 + bx + c$, when $a \neq 0$. If a is multiplied by 3, what is true of the graph of the resulting parabola?

- 1) The vertex is 3 units above the vertex of the original parabola.
- 2) The new parabola is 3 units to the right of the original parabola
- 3) The new parabola is wider than the original parabola.
- 4) The new parabola is narrower than the original parabola.

EX5: Melissa graphed the equation $y = x^2$ and Dave graphed the equation $y = -3x^2$ on the same coordinate grid. What is the relationship between the graphs that Melissa and Dave drew? Both parabolas touching the origin, axis of symmetries are $x=0$ with 1 solution, Dave's is skinnier and faces down, Melissa's faces up.

EX6: The graph of a parabola is represented by the equation $y = ax^2$ where a is a positive integer. What happens to the new parabola if a is multiplied by 2? What if multiplied by $\frac{1}{2}$? It'll become narrower.

It'll become wider.