

Warm-up 3-26

1. Write about some things that you did on break.

2. Evaluate $x^2 + 5x$ for $x = 4$ and $x = -3$

3. Generate ordered pairs for the function $y = x^2 + 2$ with the given domain.

D: $\{-2, -1, 0, 1, 2\}$

Warm-up 3-26

1. Write about some things that you did on break.

2. Evaluate $x^2 + 5x$ for $x = 4$ and $x = -3$

$$(4)^2 + 5(4)$$

$$16 + 20 = \textcircled{36}$$

$$(-3)^2 + 5(-3)$$

$$9 - 15 = \textcircled{-6}$$

$$(-3)^2 = (-3)(-3)$$

3. Generate ordered pairs for the function $y = x^2 + 2$ with the given domain. (x, y)

D: $\{-2, -1, 0, 1, 2\}$

$$\textcircled{(-2, 6) (-1, 3) (0, 2) (1, 3) (2, 6)}$$

$$y = (-2)^2 + 2$$

$$= 6$$

$$y = (0)^2 + 2$$

$$= 2$$

$$y = (2)^2 + 2$$

$$= 6$$

$$y = (-1)^2 + 2$$

$$= 3$$

$$y = (1)^2 + 2$$

$$= 3$$

Today's Goals

I can

- identify Quadratic functions
- graph a quadratic function
- determine if a quadratic opens upward or downward
- find the minimum and maximum of quadratic functions
- find the domain and range of a quadratic function

Section 10.1: Identify Quadratic Functions

Quadratic function: an expression or equation with a degree of 2.

- $y = ax^2 + bx + c$ where $a \neq 0$
- graph is always a parabola
- has a constant 2nd difference (for y)

$$y = 2x^2 + 3x$$

Determine if the function is Quadratic

From a Table:

x	y
-4	8
-2	2
0	2
2	2
4	8

Differences between rows: -6, -2, +2, +6
 Second differences: +4, +4, +4
 (yes)

From an Equation:

$$\begin{array}{r}
 y + x = 20 \\
 \underline{-x \quad -x} \\
 y = -x + 20
 \end{array}$$

(NO)

$$\begin{array}{r}
 y - 10x^2 = 9 \\
 \underline{+10x^2 + 10x^2} \\
 y = 10x^2 + 9
 \end{array}$$

(yes)

Examples

Determine if the following functions are quadratic.

$\{(-2, 9), (-1, -2), (0, 1), (0, -1), (1, 0), (2, 7)\}$

NO

$$y = 7x + 3$$

NO

$$2y + 2x^2 = 6x + 5$$

$$\underline{-2x^2 \quad -2x^2}$$

yes

$$\underline{2y = -2x^2 + 6x + 5}$$

$$\underline{y = -x^2 + 3x + 2.5}$$

x	y
-2	9
-1	-2
0	1
0	-1
1	0
2	7

Handwritten annotations: Blue arrows show differences between consecutive y-values: $9 \rightarrow -11$, $-2 \rightarrow +3$, $1 \rightarrow -2$, $-1 \rightarrow +1$, $0 \rightarrow +7$. Green arrows show second differences: $-11 \rightarrow +14$, $+3 \rightarrow -5$, $-2 \rightarrow +7$. The points $(0, 1)$ and $(0, -1)$ are circled in red.

Try These!

1. $\{(-2, 4), (-1, 1), (0, 0), (1, 1), (2, 4)\}$

2. $y + x = 2x^2$

Try These!

1. $\{(-2, 4), (-1, 1), (0, 0), (1, 1), (2, 4)\}$

yes

x	y
-2	4
-1	1
0	0
1	1
2	4

$\rightarrow -3 \rightarrow 2$
 $\rightarrow -1 \rightarrow 2$
 $\rightarrow +1 \rightarrow 2$
 $\rightarrow +3$

2. $y + \cancel{x} = \frac{2x^2}{\cancel{-x}}$

yes

$y = 2x^2 - x$

Graphing Quadratic Functions using a Table

Use a table of values to graph each quadratic function.

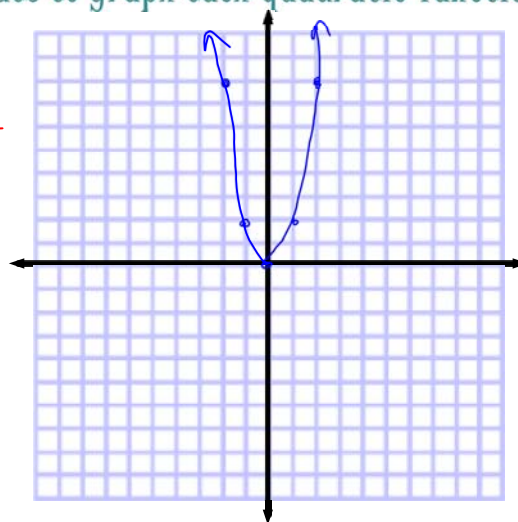
x	y
-2	8
-1	2
0	0
1	2
2	8

$$y = 2x^2$$

$$y = 2(-2)^2$$

$$= 2(4)$$

$$= 8$$



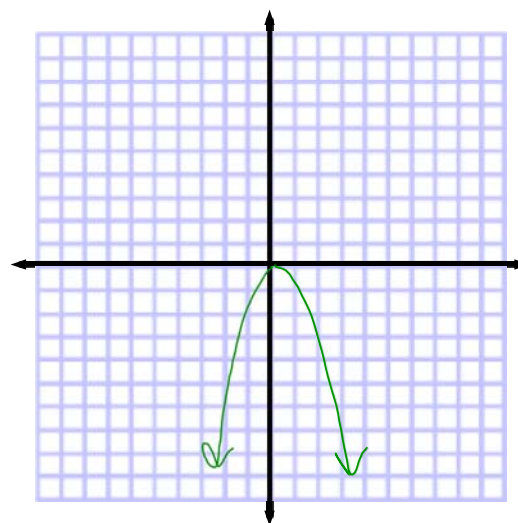
$$y = -4x^2$$

x	y
-2	-16
-1	-4
0	0
1	-4
2	-16

$$y = -4(-2)^2$$

$$= -4(4)$$

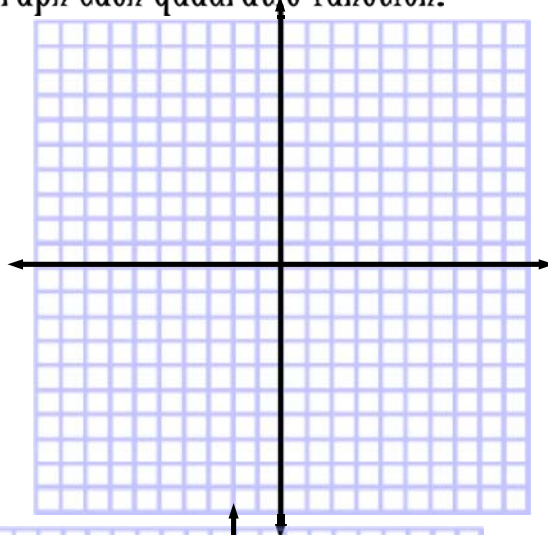
$$= -16$$



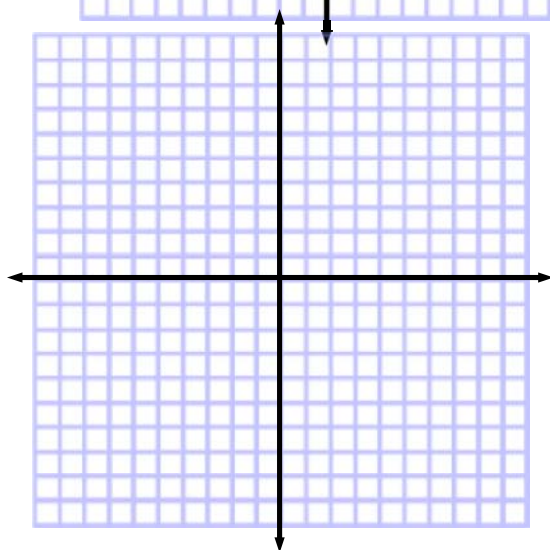
Try These!!

Use a table of values to graph each quadratic function.

$$y = \frac{1}{3}x^2$$



$$y = -2x^2$$

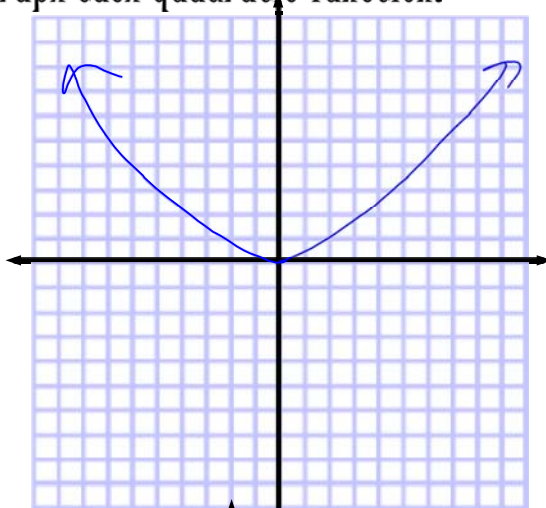


Try These!!

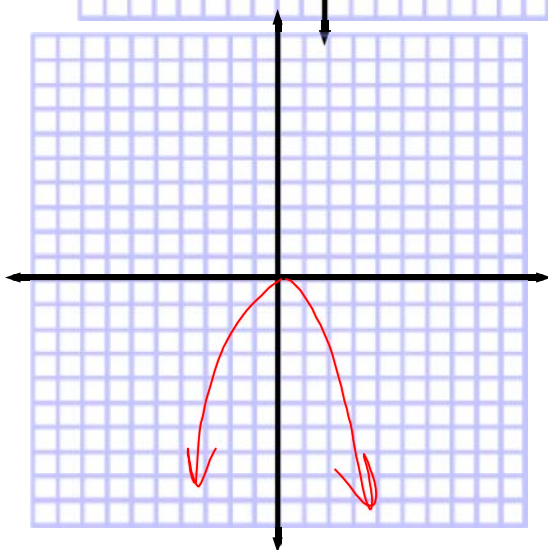
Use a table of values to graph each quadratic function.

$$y = \frac{1}{3}x^2$$

$$(1/3)x^2$$



$$y = -2x^2$$



Discuss with your neighbor:

Do you notice a pattern forming with the functions and their graphs?

If yes, Explain. If no, Explain.



Identifying the direction of a Parabola

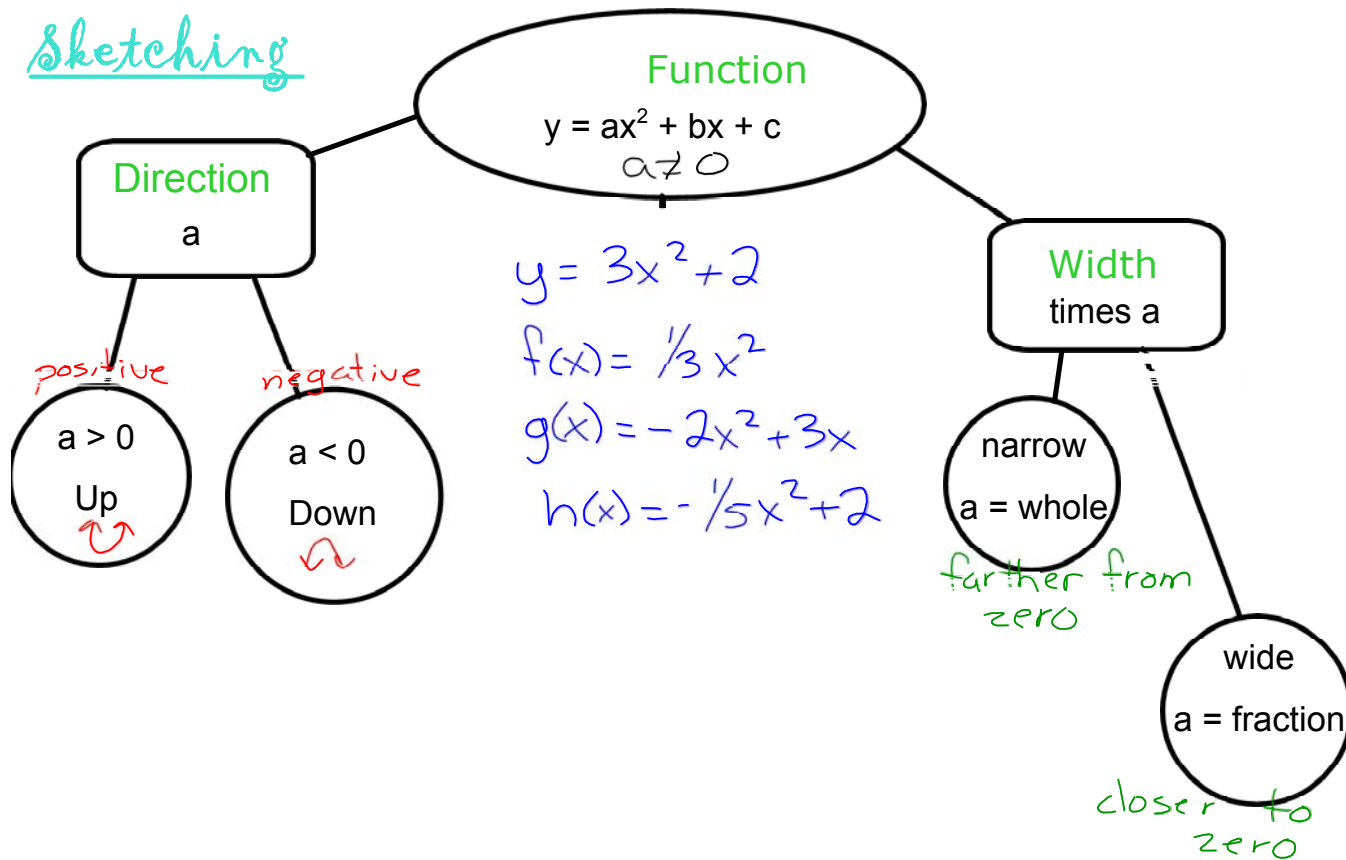
$$y = 4x^2$$

up (narrow)

$$\begin{array}{r} 2x^2 + y = 5 \\ -2x^2 \quad -2x^2 \\ \hline \end{array}$$

$$y = -2x^2 + 5$$

down (narrow)



$$y = 3x^2 + 8x \quad \text{narrowest} \rightarrow \text{widest}$$

$$f(x) = -2x^2 + 3$$

$$g(x) = -\frac{1}{8}x^2$$

$$h(x) = -\frac{1}{2}x^2 + 3x$$

$$y = \underline{+3}x^2 + 8x \quad \text{up}$$

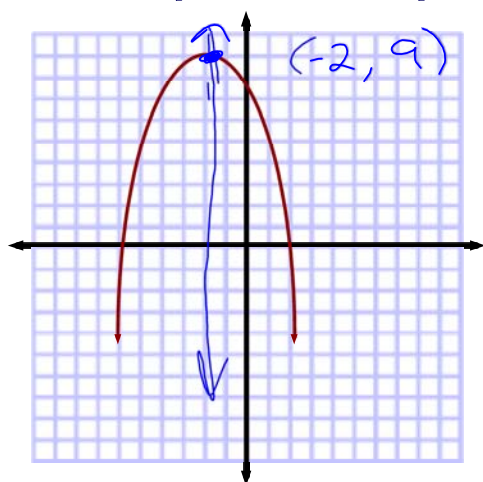
$$f(x) = \underline{-2}x^2 + 3 \quad \text{down}$$

$$h(x) = \underline{-\frac{1}{2}}x^2 + 3x \quad \text{down}$$

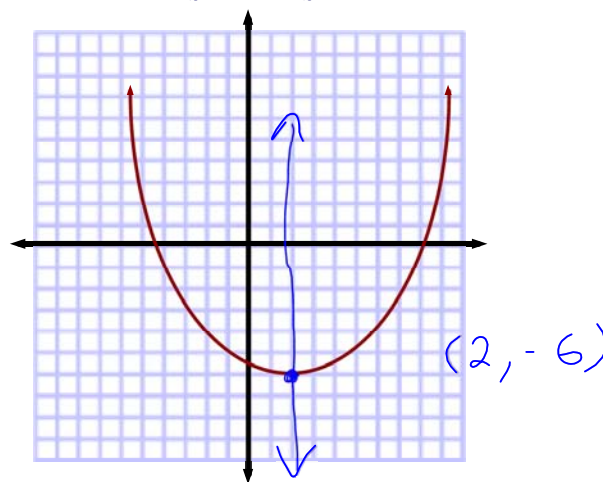
$$g(x) = \underline{-\frac{1}{8}}x^2 \quad \text{down}$$

Maximum and Minimum Values

Vertex - the point where the parabola crosses its axis of symmetry (max or min)

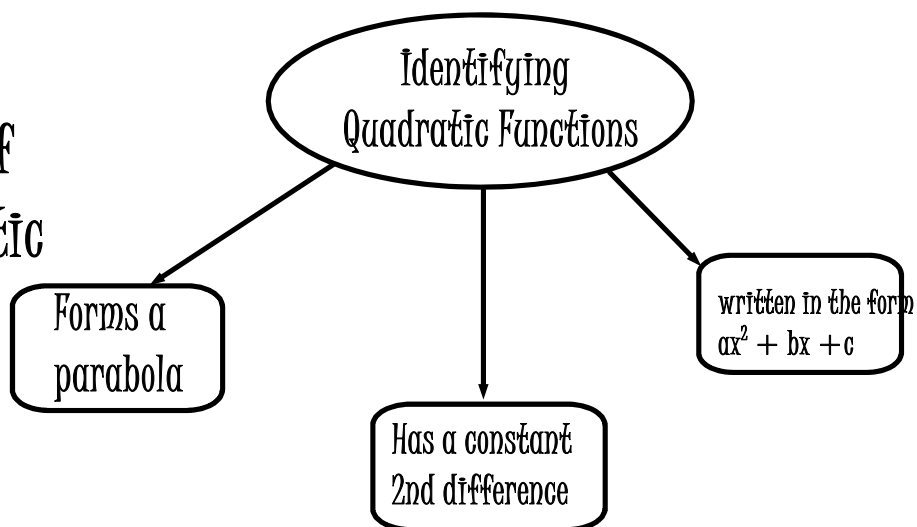


Vertex



Review

Describe the ways of identifying quadratic functions



Homework

pg. 526 #1-15 (odd)